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## Mathematics

Quarter 3 - Module 2:
Formulating Rules; Expression or Equation

Name of Learner:
Grade \& Section:
Name of School:

## What I Need to Know

The module contains one lesson:
Lesson 2: Formulating rules in finding Nth Term and Differentiating Expression from Equation.
After going through this module, you are expected to:

1. Formulate the rule in finding the nth term using different strategies (looking for a pattern, guessing and checking, working backwards)
2. Differentiate expression from equation


## What I Know

Let us know of what you already know about this lesson
Directions: Supply the next three letters, figures, symbols, or combination of numbers and letters in the following patterns.

1. $2 \mathrm{a}, 3 \mathrm{~b}, 4 \mathrm{c}$, $\qquad$
4.z,y,x,w,z $\qquad$
2. $2,4,6,8$ $\qquad$
3. $z, z^{3}, z^{5}$, $\qquad$
4. $5,7,9$, $\qquad$ , ,

Directions: Thumbs up if the statement is true, thumbs down if the statement is false. Blacken the icons for your answer.

1. Expression is a phrase. $a \Omega \square \sqrt[3]{ }$
2. Equation is a sentence. $\square$

3. Equation has an equal sign. $\sim$
4. Equation has two sides, left and right.
5. Expression has two sides, left and right. $\sim \Omega$

## What's In

A plane figure is two-dimensional, and a solid figure is three-dimensional. The difference between plane and solid figures is in their dimensions. Where a square is a plane figure, its 3D counterpart, the cube, is a solid figure. The same comparison exists between a circle, or plane figure, and a sphere, a solid figure.

Directions: Complete the Table

| Figure | Name of a Figure | Real object |
| :---: | :---: | :---: |
| 1. $\ldots \ldots$ |  | Jewelry Box |
| 2. |  |  |
| 3. | Cube |  |
| 4. |  |  |
| 5. |  |  |



## What's New

Poem with Scout and ESP Integration

Finding out Nth Term Rule
Finding out the Nth Term Rule so easy topic at school
We diligent scouters study about in all
And we will make sure, know the rule
So we have learnt the nth term rule
First, work out the difference and work it out again
Write down the number followed by an $\mathbf{N}$
Then work backwards to find the exact $n$th term

## Expression and Equation

Expression and equation with symbols and letters Equations has two expressions, equal to each other. Don't be lazy, both get easier.

Coz we, diligent scouters
Expression of $2 x-5$, look for a signs to get a clue Minus addition and multiplication that are true Equation $2 x-5=5$, equals we have seen through

So scouters see the difference too.

## Finding out the nth Term Rule

The nth Term of a Sequence
A sequence is a set of numbers written in a special order by the application of a definite rule. Each number in the sequence is called a term.

## Example 1

| Sequence | Nth term Rule | Next Three terms |
| :--- | :--- | :--- |
| a. $\quad 7, \quad 10, \quad 13, \quad 16$ | To get this nth term rule see <br> the steps below | $19,22,25$ |

## To find Nth term Rule

Steps are follow:

## Step 1: See the difference



Every term after the first is obtained by adding 3, so write 3n $\downarrow$
Step 2: Multiply the counting numbers by 3 or shall we say multiples by 3

## Counting numbers

The set of numbers $1,2,3,4,5 \ldots$...without (zero) is called counting numbers

$$
3(1)=\mathbf{3} \quad 3(2)=\mathbf{6} \quad 3(3)=\mathbf{9} \quad 3(4)=\mathbf{1 2}
$$

Write all the products on the given sequence number

Step 3: Working backwards by subtracting the products from the given sequence
$7-3=4$


You will notice the pattern, if all the products will be added by 4 you can get the given sequence number.
$3+4=7$
$6+4=10$
$9+4=13$
$12+4=16$

## To Check:

Substitute counting number to $\mathbf{N}$
Since our nth term rule is $3 n+4$
Let $\mathbf{N}$ represents counting number
Counting Numbers 1,2,3,4 $5 \ldots$.

| $3 n+4$ | $3 n+4$ | $3 n+4$ | $3 n+4$ |
| :--- | :--- | :--- | :--- |
| $3(1)+4$ | $3(2)+4$ | $3(3)+4$ | $3(4)+4$ |
| $3+4=\mathbf{7}$ | $6+4=\mathbf{1 0}$ | $9+4=\mathbf{1 3}$ | $12+4=\mathbf{1 6}$ |

Example 2:

| Sequence |  |  |  | Nth term Rule | Next Three terms |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| a. 22 | 19 | 16 | 13 | 10 | $-3 n+25$ | $7,4,1$ |

Step 1: See the difference


Step 3: Working backwards by subtracting the products from the given sequence

$$
22-(-3)=25
$$



So write $\mathbf{+ 2 5}$
Nth term Rule is $\mathbf{- 3 n + 2 5}$
Checking:

| $-3 n+25$ | $-3 n+25$ | $-3 n+25$ | $-3 n+25$ | $-3 n+25$ |
| :--- | :--- | :--- | :--- | :--- |
| $-3(1)+25$ | $-3(2)+25$ | $-3(3)+25$ | $-3(4)+25$ | $-3(5)+25$ |
| $=22$ | $=19$ | $=16$ | $=13$ | $=15$ |

Example 3:

| Sequence | Nth term Rule | Next Three terms |
| :--- | :---: | :---: |
| $\frac{\mathbf{1}}{\mathbf{6}}, \frac{\mathbf{1}}{\mathbf{1 0}}, \frac{\mathbf{1}}{\mathbf{1 4}}, \frac{\mathbf{1}}{\mathbf{1 8}}$, | $\frac{1}{4 n+2}$ | $\frac{\mathbf{1}}{22}, \frac{\mathbf{1}}{\mathbf{2 6}}, \frac{\mathbf{1}}{\mathbf{1 4}}, \frac{\mathbf{1}}{\mathbf{3 0}}$, |

Step 1: See the difference

$$
\frac{1}{6}, \frac{1}{10}, \frac{1}{14}, \frac{1}{18},
$$

Step 2: Multiples of 4

Step 3: Working backwards by subtracting the products from the given sequence


This example we have no constant difference

| Sequence | Nth term Rule | Next Three terms |
| :---: | :---: | :---: |
| $\mathbf{3 , ~ 9 , ~ 1 7 , ~ 2 7 ~}$ | $\mathrm{n}^{2}+3 \mathrm{n}-1$ | $39 \quad 5369$ |

## Example 4

Step 1: See the difference

In this case we have $2^{\text {nd }}$
difference write $\mathbf{n}^{2}$

Step 2: Divide the second difference by

$$
3, \quad 9, \quad 17, \quad 27
$$




Write the quotient 1 before the $\mathrm{n}^{2=}$ $1 n^{2}$

## Assuming

If the second difference is 8 we can have $\frac{8}{2}$
$=4$
It becomes $\mathbf{4 n}^{\mathbf{2}}$

## Step 3

Draw a table

| $\mathbf{n}$ | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| sequence | 3 | 9 | 17 | 27 |
| $\mathbf{1 n}^{\mathbf{2}}$ | $(1)^{1}=1$ | $(2)^{2}=4$ | $(3)^{2}=9$ | $(4)^{2}=16$ |
| Subtraction | $3-1$ | $9-4$ | $17-9$ | $27-16$ |
|  | 2 | 5 | 8 | 11 |


-1 might be constant if we have this kind of example

## Checking:

| $1 n^{2}+3 n-1$ | $1 n^{2}+3-1$ | $1 n^{2}+3 n-1$ | $1 n^{2}+3 n-1$ |
| :--- | :--- | :--- | :--- |
| $1(1)^{2}+3(1)-1$ | $1(2)^{2}+3(2)-1$ | $1(3)^{2}+3(3)-1$ | $1(4)^{2}+3(4)-1$ |
| $1+3-1$ | $4+6-1$ | $9+9-1$ | $16+12-1$ |
| $=3$ | $=9$ | $=17$ | $=27$ |

## Definitions:

A numerical expression is an expression that combines numbers and one or more operation symbols
A variable is any letter or symbol that represents a number.
A constant has a fixed value that does not change.
An algebraic expression is a mathematical phrase that used variables, numerals, and operation symbols.
An algebraic equation is a mathematical sentence with an equal sign (=) which shows that two expression on either side are equal.

## Differentiates Expression from Equation

Comparison Chart

| BASIS FOR COMPARISON | EXPRESSION | EQUATION |
| :---: | :---: | :---: |
| Meaning | Expression is a mathematical phrase which combines, numbers, variables and operators to show the value of something. | An equation is a mathematical statement wherein two expressions are set equal to each other. |
| What is it? | A sentence fragment, that stands for a single numerical value. | A sentence that shows equality between two expressions. |
| Result | Simplification | Solution |
| Relation symbol | No | Yes, equal sign (=) |
| Sides | One sided | Two sided, left and right |
| Answer | Numerical value | Assertion, i.e. true or false. |
| Example | $7 \mathrm{x}-2(3 x+14)$ | $7 \mathrm{x}-5=19$ |
|  | An expression is a PHRASE, a sentence fragment. | An equation is a SENTENCE. |

## What's More

A. Directions: Differentiates expression from equation. Put your answer in the Venn diagram.

B. Directions: Find an expression by formulating the rule of the nth term. Connect each airplane to the clouds that corresponds to its correct answer.
1.

5.


## What I Have Learned

## Directions: Fill in the blanks

1. What are the missing numbers in the sequence? $\frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \ldots, \quad, \frac{7}{8}$
2. Complete the pattern $20,16,12,8$ $\qquad$ , $\qquad$ , $\qquad$
For items 3-5
3. How many members in the $5^{\text {th }}$ troop if the first troop has 8 members, the second troop has 10 members, and third troop has 12. $\qquad$
4. Which troop has 22 members? $\qquad$ .
5. What is the common difference? $\qquad$
6. -10. Directions: Select your answer from the box

| $3 k+7=34$ | $3 n+5$ | $5 m+2$ | $2 n-13=9$ | $2 n+5$ |
| :--- | :--- | :--- | :--- | :--- |


| Expression | Equation |
| :---: | :---: |
|  |  |

## What I Can Do

A. Directions: Formulate the rule in finding the nth term. Then find the next three terms in each sequence.
a. $3,5,7,9$ $\qquad$ , $\qquad$ Rule: $\qquad$
b. $\frac{2}{3}, \frac{3}{4}, \frac{4}{5}$ $\qquad$ , $\qquad$ ,

Rule: $\qquad$
c. $-2,-4,-6$ $\qquad$ Rule: $\qquad$
d. $5,10,15,20$ $\qquad$ , $\qquad$ , $\qquad$ Rule: $\qquad$
e. $3,6,9,12$ $\qquad$ , $\qquad$ , $\qquad$ Rule: $\qquad$
B. Directions: Give at least 3 examples of expression and 2 examples of equation.

Directions: Read carefully and put your answer on the blank.

1. Carmi gets a starting salary of $13,000.00$ a month and an increase of 500.00 annually. What will be her salary during the fifth year? $\qquad$
Solutions:
2. Mrs. Torres increased her son's allowance who is studying in a university. She gave him $3,000.00$ on the first month, $3,300.00$ on the second month, 3600.00 on the third month and so on. How much will her son receive on the $7^{\text {th }}$ month?
Solutions:
3. A pile of blocks has 40 blocks in the bottom row, 36 blocks in the second row, and 32blocks on the third row and so on until there are only 4 blocks on the top of row. How many blocks are there in the $7^{\text {th }}$ row?
Solutions:
4. What is the $5^{\text {th }}$ sequence if the $n$th term rule is $3 n-9$ $\qquad$ ?
Solutions:
5. Formulate the rule in finding the nth term of this sequence $40,36,32,30$

Solutions:

1. Has a relation symbol $\qquad$
2. Consist of two expressions $\qquad$
3. $10(5)-5(2)=40$ is an example of $\qquad$
4. A number less than five $\qquad$
5. Ten equals five less than a number $\qquad$

## Additional Activities:

Find an expression for the nth term in the sequence $-6,-3,2,9$

## References

Perez, Marjoseph H., Donnel P. Placer, Jaime R. Burgos. $21^{\text {st }}$ Century MATHletes 6. edited by Mercurio T. Elenzano, EdD, Chin Uy, Ph.D..Quezon City.Vibal Group, Inc.. 2016

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